

SOLUTIONS SET - 1
MATHEMATICS - CLASS X

1. $84 = 2^2 \times 3 \times 7$
 \therefore Prime factors of 84 are 2, 3 and 7.
2. Sum of zeroes = $-5 + 4 = -1$
Product of zeroes = $-5 \times 4 = -20$
 \therefore Required polynomial = $x^2 - (-1)x + (-20)$
 $= x^2 + x - 20$

3. Given equation is $2x + 3y - 13 = 0$
For $x = 2, y = 3$
L.H.S becomes $2(2) + 3(3) - 13$
 $= 4 + 9 = 13$
 $= 13 - 13 = 0$
 $= \text{R.H.S}$
Hence, $x = 2, y = 3$ is a solution of the given equation.

4. Here, first term = $\sqrt{2}$
Second term = $\sqrt{8}$
 \therefore Common difference = $\sqrt{8} - \sqrt{2} = \sqrt{2}$
 \therefore Next term = $\sqrt{18} + \sqrt{2} = 4\sqrt{2}$

5. $\cos A = \frac{3}{5}$
 $\therefore \sin A = \frac{4}{5}$
Now, $\cot A = \frac{\cos A}{\sin A} = \frac{3}{4}$
 $\therefore 9 \cot^2 A - 1 = 9 \left(\frac{3}{4}\right)^2 - 1$
 $= \frac{81 - 16}{16}$

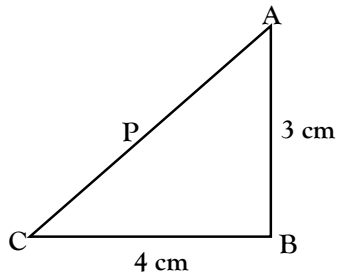
$$= \frac{65}{16}$$

6. Probability of losing = 1 - probability of winning

$$= 1 - \frac{5}{11}$$

$$= \frac{6}{11}$$

7.



By Pythagoras theorem

$$AC = \sqrt{AB^2 + BC^2} = 5 \text{ cm}$$

$$\text{Now } AP = \frac{1}{2} AC = \frac{5}{2} = 2.5 \text{ cm}$$

8. Let BC touches the circle at point K

Now, $AP = AQ = 10 \text{ cm}$

and $BP = BK \dots (i)$

and $CQ = CK \dots (ii)$

$AB = AP - BP$

$AC = AQ - QC$

and $BC = BK + KC$

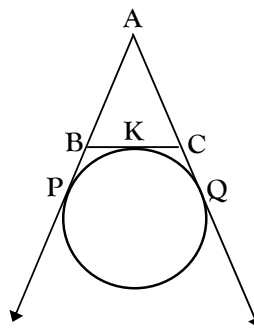
Perimeter of $\triangle ABC = AB + BC + AC$

$= AP - BP + BK + KC + AQ - QC$

$= AP + AQ \dots [\text{using (i) and (ii)}]$

$= 10 + 10$

$= 20 \text{ cm}$



9. Let $r_1 = 3$ cm, $r_2 = 4$ cm and R be the radius of the required circle A.T.Q.

$$\pi R^2 = \pi r_1^2 + \pi r_2^2$$

$$= \pi(r_1^2 + r_2^2)$$

$$\therefore R^2 = r_1^2 + r_2^2$$

$$= 4^2 + 3^2$$

$$= 25$$

$$\therefore R = 5 \text{ cm}$$

10. Median = 20.5

11. For zeros the quadratic polynomial is equated to 0.

$$\text{i.e. } 2x^2 - 9 - 3x = 0$$

$$\text{or } 2x^2 - 3x - 9 = 0$$

$$\Rightarrow 2x^2 - 6x + 3x - 9 = 0$$

$$\Rightarrow (2x + 3)(x - 3) = 0$$

Now, either $2x + 3 = 0$ or $x - 3 = 0$

$$\Rightarrow 2x = -3 \Rightarrow x = -\frac{3}{2}$$

$$\Rightarrow x = -\frac{3}{2}$$

So, zeros of the equation are $-\frac{3}{2}$ and 3

Verification of relation

Here in the equation by equating with general equation we get

$$a = 2, b = -3, c = -9$$

$$(i) \quad \text{Now sum of zeros} = -\frac{3}{2} + 3 = \frac{-3 + 6}{2} = \frac{3}{2} \text{ and } -\frac{b}{a} = -\frac{(-3)}{2} = \frac{3}{2}$$

$$\text{i.e. sum of zeros} = -\frac{b}{a}$$

$$(ii) \quad \text{Product of zeros} = x_1 \cdot x_2 = -\frac{3}{2} \times 3 = -\frac{9}{2}$$

$$\text{Also } \frac{c}{a} = -\frac{9}{2}$$

$$\text{i.e. product of zeros} = \frac{c}{a} = \frac{\text{coefficient constt}}{\text{coefficient of } x^2}$$

12. Given: $3 \cot \theta = A \Rightarrow \cot \theta = \frac{4}{3} = \frac{\text{Base}}{\text{perpendicular}}$

So in ΔABC , using Pythagoras

$$AC^2 = AB^2 + BC^2 = (4k)^2 + (3k)^2$$

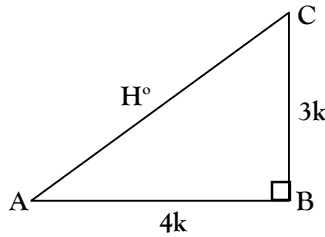
$$= (16 + 9)k^2 = 25k^2$$

$$AC = \sqrt{25k^2} = 5k \text{ (Neglecting - Negative as length can't be less than zero)}$$

$$\text{So } \sin \theta = \frac{3k}{5k} \text{ and } \cos \theta = \frac{4k}{5k}$$

$$\frac{5 \sin \theta - 3 \cos \theta}{5 \sin \theta + 3 \cos \theta} = \frac{5 \times \frac{3}{5} - 3 \times \frac{4}{5}}{5 \times \frac{3}{5} + 3 \times \frac{4}{5}}$$

$$= \frac{15 - 12}{15 + 12} = \frac{3}{27} = \frac{1}{9}$$



OR

$$\left(\frac{\tan 20^\circ}{\operatorname{cosec} 70^\circ} \right)^2 + \left(\frac{\cot 20^\circ}{\sec 70^\circ} \right)^2 + 2 \tan 15^\circ \cdot \tan 45^\circ \cdot \tan 75^\circ$$

$$\Rightarrow \left(\frac{\sin 20^\circ}{\cos 20^\circ} \times \sin 70^\circ \right)^2 + \left(\frac{\cos 20^\circ}{\sin 20^\circ} \times \cos 70^\circ \right)^2 + 2 \tan 15^\circ \cdot 1 \times \tan (90^\circ - 15^\circ)$$

$$= \left(\frac{\sin 20^\circ}{\cos 20^\circ} \times \cos 20^\circ \right)^2 + \left(\frac{\cos 20^\circ}{\sin 20^\circ} \times \sin 20^\circ \right)^2 + 2 \tan 15^\circ \cdot \cot 15^\circ$$

$$\left\{ \begin{array}{l} \text{using formula} \\ \sin (90^\circ - \theta) = \cos \theta \\ \cos (90^\circ - \theta) = \sin \theta \\ \tan (90^\circ - \theta) = \cot \theta \end{array} \right.$$

$$= (\sin^2 20^\circ + \cos^2 20^\circ) + 2 \cdot \tan 15^\circ \times \frac{1}{\tan 15^\circ} \quad \left\{ \text{using } \cot \theta = \frac{1}{\tan \theta} \right\}$$

$$= 1 + 2 = 3 \quad \left\{ \text{using } \sin^2 \theta + \cos^2 \theta = 1 \right\}$$

13. Given: $A(x_1, y_1) = (1, k)$, $B(x_2, y_2) = (4, -3)$

$$C(x_3, y_3) = (-9, 7)$$

And Area(ΔABC) = 15 square units

We know Area of a triangle with coordinates (x_1, y_1) , (x_2, y_2) , (x_3, y_3) is

$$\text{Area} = \frac{1}{2} |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)|$$

$$\Rightarrow 15 = \frac{1}{2} |1(-3 - 7) + 4(7 - k) - 9(k + 3)|$$

$$30 = |-10 + 28 - 4k - 9k - 27|$$

$$\text{or } |-13k - 9| = 30$$

\Rightarrow either

$$-13k - 9 = 30 \quad \text{or} \quad -(-13k - 9) = 30$$

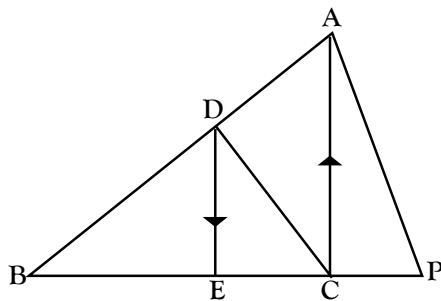
$$-13k = 39 \quad \quad \quad 13k + 9 = 30$$

$$k = -\frac{39}{13} = -3 \quad \quad \quad 13k = 21$$

$$k = 3 \quad \quad \quad k = \frac{21}{13}$$

$$\Rightarrow k = 3 \text{ or } \frac{21}{13}$$

14.



Given: $DE \parallel AC$ and $\frac{BE}{EC} = \frac{BC}{CP}$... (i)

To prove: $DC \parallel AP$

Proofs: In $\triangle ABC$, $DE \parallel AC$ (Given)

$$\Rightarrow \frac{BE}{CE} = \frac{BD}{DA} \quad \dots \text{ (ii)}$$

A line parallel to one side of a triangle divides the other two sides in the same ratio

Also $\frac{BE}{CE} = \frac{BC}{CP}$ (Given)

So we have $\frac{BD}{AD} = \frac{BC}{CP}$... (iii)

Now in $\triangle ABP$; $\frac{BD}{AD} = \frac{BC}{CD}$ (just proved)

$$\Rightarrow DC \parallel AP$$

(A line dividing two sides of a triangle in the same ratio is parallel to the third side)

15. Total number of cards in the box = 65

(i) Number of cards of one digit = (6, 7, 8, 9) = 4

$$\text{Probability of 1 digit number} = \frac{4}{65}$$

(ii) Total numbers divisible by 5 = (10, 15, 20, 25, 30, 35, 40, 45, 50, 55, 60, 65 and 70) = 13

$$\text{Probability of number divisible by 5} = \frac{13}{65} = \frac{1}{5}$$

16. $72 = 2^3 \times 3^2$

$$126 = 2 \times 3^2 \times 7$$

$$168 = 2^3 \times 3 \times 7$$

$$\text{HCF} = 2 \times 3 = 6$$

$$\text{LCM} = 2^3 \times 3^2 \times 7 = 504$$

$$\text{HCF} \times \text{LCM} = 2 \times 3 \times 2^3 \times 3^2 \times 7 = 2^4 \times 3^3 \times 7$$

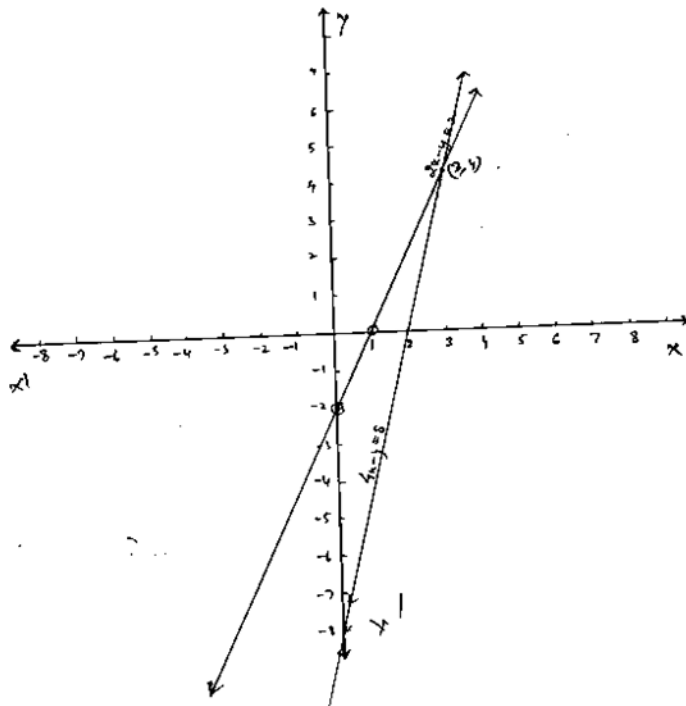
$$\text{Product of numbers} = 2^3 \times 3^2 \times 2 \times 3^2 \times 7 \times 2^3 \times 7 = 2^7 \times 3^5 \times 7^2$$

∴ $\text{HCF} \times \text{LCM} \neq \text{Product of numbers}$.

17. $2x - y = 2$

$$4x - y = 8$$

The point of intersection is (3, 4).



18. $(a - b)x + (a + b)y = a^2 - 2ab - b^2$ (1)

$(a + b)x + (a + b)y = a^2 + b^2$ (2)

Subtracting (1) from (2), we get

$$2bx = 2b^2 + 2ab$$

$$\Rightarrow x = a + b$$

Substituting in (1)

$$(a - b)(a + b) + (a + b)y = a^2 - 2ab - b^2$$

$$\Rightarrow (a + b)y = -2ab$$

$$\Rightarrow y = \frac{-2ab}{a + b}$$

OR

For real and distinct roots, $D > 0$

$$\therefore 4(1 + 2m)^2 - 8m(3 + 2m) > 0$$

$$4 + 16m^2 + 16m - 24m - 16m^2 > 0$$

$$4 - 8m > 0$$

$$\Rightarrow m < \frac{1}{2}$$

For equal roots, $D = 0$

$$\Rightarrow m = \frac{1}{2}$$

19. L.H.S. = $\frac{\cos \theta - \sin \theta + 1}{\cos \theta + \sin \theta - 1}$

$$= \frac{\frac{\cos \theta}{\sin \theta} - \frac{\sin \theta}{\sin \theta} + \frac{1}{\sin \theta}}{\frac{\cos \theta}{\sin \theta} + \frac{\sin \theta}{\sin \theta} - \frac{1}{\sin \theta}}$$

$$= \frac{\cot \theta - 1 + \operatorname{cosec} \theta}{\cot \theta + 1 - \operatorname{cosec} \theta}$$

$$= \frac{\cot \theta - (\operatorname{cosec}^2 \theta - \cot^2 \theta) + \operatorname{cosec} \theta}{\cot \theta + 1 - \operatorname{cosec} \theta}$$

$$= \frac{\cot \theta + \operatorname{cosec} \theta - (\operatorname{cosec} \theta - \cot \theta)(\operatorname{cosec} \theta + \cot \theta)}{\cot \theta + 1 - \operatorname{cosec} \theta}$$

$$= \frac{(\cot \theta + \operatorname{cosec} \theta)[1 - \operatorname{cosec} \theta + \cot \theta]}{[1 - \operatorname{cosec} \theta + \cot \theta]}$$

$$= \cot \theta + \operatorname{cosec} \theta$$

$$= \text{R.H.S.}$$

OR

$$\text{R.H.S.} = \frac{1}{\tan \theta + \cot \theta}$$

$$= \frac{1}{\frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta}}$$

$$= \frac{1}{\frac{\sin^2 \theta + \cos^2 \theta}{\cos \theta \sin \theta}}$$

$$\text{Also, R.H.S.} = (\operatorname{cosec} \theta - \sin \theta) (\sec \theta - \cos \theta)$$

$$= \left(\frac{1}{\sin \theta} - \sin \theta \right) \left(\frac{1}{\cos \theta} - \cos \theta \right)$$

$$= \frac{(1 - \sin^2 \theta)}{\sin \theta} \frac{(1 - \cos^2 \theta)}{\cos \theta}$$

$$= \frac{\cos^2 \theta \sin^2 \theta}{\sin \theta \cos \theta}$$

$$= \cos \theta \sin \theta$$

$$\text{Hence, R.H.S.} = \text{L.H.S.}$$

20. The required A.P. is 10, 13, 16,,97

It is an A.P with $a = 10$, $d = 3$ and $n = 30$

$$\therefore S = \frac{n}{2} [2a + (n - 1)d] = \frac{30}{2} [2 \times 10 + 29 \times 3] = 1605$$

21. P is the mid-point of the line segment joining (2, -1) and (5, -6)

$$\therefore \text{Co-ordinates of P are } \left(\frac{7}{2}, \frac{-7}{2} \right)$$

P lies on $2x + 3y + k = 0$

$$\therefore 2 \times \frac{7}{2} + 3 \left(\frac{-7}{2} \right) + k = 0$$

$$7 - 14 + k = 0$$

$$\Rightarrow k = 7$$

22. Given: A triangle ABC with AD as median

Construction : Draw AM perpendicular to BC.

$$\text{In } \triangle ABM, AB^2 = AM^2 + BM^2$$

$$= (AD^2 - DM^2) + (BD + DM)^2$$

$$AB^2 = AD^2 + BD^2 + 2BD \cdot DM \quad \dots (i)$$

In $\triangle AMC$,

$$AC^2 = AM^2 + MC^2$$

$$AC^2 = (AD^2 - DM^2) + (CD - DM)^2$$

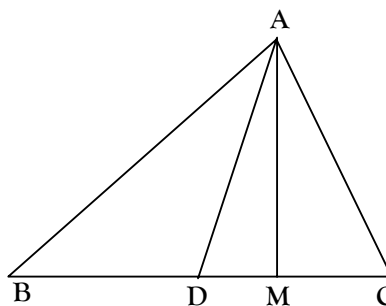
$$AC^2 = AD^2 + CD^2 - 2CD \cdot DM \quad \dots (ii)$$

Adding (i) and(ii)

$$AB^2 + AC^2 = AD^2 + BD^2 + 2BD \cdot DM + AD^2 + CD^2 - 2CD \cdot DM$$

Since, $BD = CD$

$$\Rightarrow AB^2 + AC^2 = 2(AD^2 + BD^2)$$



OR

Given: A triangle ABC with an acute angle $\angle A$ and lines BD and CE perpendicular on lines AC and AB respectively.

To prove: $AB \times AE = AC \times AD$

In $\triangle ABD$ and $\triangle ACE$

$$\angle A = \angle A$$

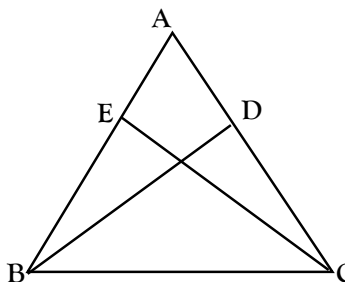
$$\angle ADB = \angle AEC = 90^\circ \quad [\text{given}]$$

Hence, $\triangle ABD \sim \triangle ACE$

$$\text{So } \frac{AC}{AB} = \frac{AE}{AD}$$

$$AC \times AD = AE \times AB$$

Hence proved



23. Let A(5, 6), B(1, 5), C(2, 1) and D(6, 2) be the vertices of the square. To show that it is a square we should use the property that all its sides should be equal and both its diagonals should also be equal.

Now,

$$AB = \sqrt{(5-1)^2 + (6-5)^2} = \sqrt{(4)^2 + (1)^2} = \sqrt{17}$$

$$BC = \sqrt{(1-2)^2 + (5-1)^2} = \sqrt{1+16} = \sqrt{17}$$

$$CD = \sqrt{(2-6)^2 + (1-2)^2} = \sqrt{16+1} = \sqrt{17}$$

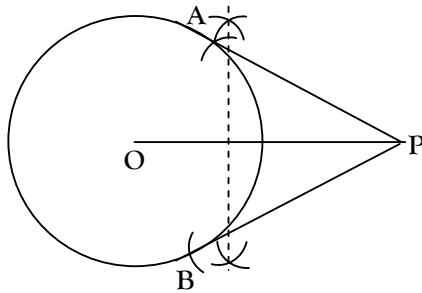
$$DA = \sqrt{(6-5)^2 + (2-6)^2} = \sqrt{1+16} = \sqrt{17}$$

$$AC = \sqrt{(5 - 2)^2 + (6 - 1)^2} = \sqrt{9 + 25} = \sqrt{34}$$

$$BD = \sqrt{(1 - 6)^2 + (5 - 2)^2} = \sqrt{25 + 9} = \sqrt{34}$$

Since, $AB = BC = CD = DA$ and $AC = BD$, all the four sides of the quadrilateral ABCD are equal and its diagonals AC and BD are also equal. Therefore ABCD is a square.

24.



PA and PB are the required tangents.

25. Radius of circle is $OA = R = 14$ cm.

Radius of circle with diameter $OD = r = 7$ cm

So area of this circle is πr^2 .

$$= \frac{22}{7} \times 7 \times 7 = 154 \text{ cm}^2.$$

$$\text{Area of the semicircle} = \frac{1}{2} (\pi R^2)$$

$$= \frac{1}{2} \times \frac{22}{7} \times 14 \times 14 = 308 \text{ cm}^2$$

Area of the shaded portion = (area of circle with radius r) + (area of semicircle with radius R) - (area of the triangle)

$$= 154 + 308 - \frac{1}{2} \times 28 \times 14$$

$$= 154 + 308 - 196 = 266 \text{ cm}^2$$

26. Let the number of persons be = n

If Rs. 6500 is divided equally then each will get = Rs. $\frac{6500}{n}$

If number of persons are increased by 15 i.e. $n + 15$ then each person will get Rs. 30 less.

So according to question.

$$\frac{6500}{n+15} = \frac{6500}{n} - 30$$

$$30 = \frac{6500}{n} - \frac{6500}{n+15}$$

$$30 = 6500 \left(\frac{1}{n} - \frac{1}{n+15} \right)$$

$$\therefore 30 = 6500 \left(\frac{15}{(n)(n+15)} \right)$$

$$(n)(n+15) = \frac{6500 \times 15}{30}$$

$$n^2 + 15n - 3250 = 0$$

$$n^2 + 65n - 50n - 3250 = 0$$

$$n(n+65) - 50(n+65) = 0$$

$$n = 50, -65$$

So number of person are 50.

OR

Let the speed of train b = v km/h

So time taken by train to cover 360 km = $\frac{360}{v}$ hours

Now if the speed is increased by 5 km/h i.e. v + 5 km/h then time reduces by one hour.

So according to question

$$\frac{360}{v} - 1 = \frac{360}{v+5}$$

$$\frac{360}{v} - \frac{360}{v+5} = 1$$

$$360 \left(\frac{1}{v} - \frac{1}{v+5} \right) = 1$$

$$\frac{360 \times 5}{(v)(v+5)} = 1$$

$$\Rightarrow (v)(v+5) = 1800$$

$$v^2 + 5v - 1800 = 0$$

$$v^2 + 45v - 40v - 1800 = 0$$

$$v(v+45) - 40(v+45) = 0$$

$$(v-40)(v+45) = 0$$

$$v = 40, -45$$

So original speed of train is 40 km/h

27. Let GH be the upper surface of the lake, C be the position of the cloud, D be its reflection in the lake and E be the eye of the observer.

Draw $EF \perp CD$ and $EG \perp GH$. Then,

$$GE = 60, \angle FEC = 30^\circ \text{ and } \angle FED = 60^\circ.$$

Clearly, $FH = GE = h$. Let height of the cloud = $HC = HD = x$.

$$\therefore FC = x - 60 \text{ and } FD = x + 60.$$

$$\text{Now, } \frac{EF}{FD} = \cot 60^\circ$$

$$\Rightarrow EF = (x + 60) \cot 60 = (x + 60) \frac{1}{\sqrt{3}}$$

$$\text{Also } \frac{EF}{FC} = \cot 30^\circ$$

$$\Rightarrow EF = (x - 60) \sqrt{3}$$

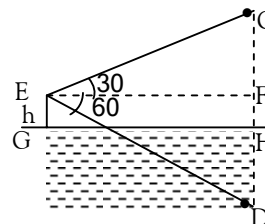
$$\therefore EF = (x - 60) \sqrt{3} = (x + 60) \frac{1}{\sqrt{3}} \quad 3(x - 60) = (x + 60)$$

$$3x - 180 = x + 60$$

$$2x = 240$$

$$x = 120$$

Height of the cloud = 120 m



28. The length of two tangents drawn from an external point to a circle are equal.

Given: Two tangents AP and AQ drawn from a point A to a circle C(O, r).

To prove: $AP = AQ$.

Construction: Join OP, OQ, and OA.

Proof: Since a tangent at any point of a circle is perpendicular to the radius through the point of contact, we have $OP \perp AP$ and $OQ \perp AQ$.

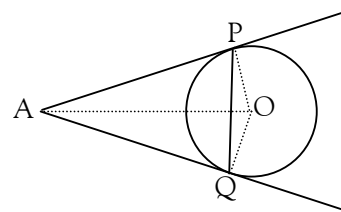
Now, in right triangles OPA and OQA, we have

$$OP = OQ \text{ (radii)}$$

$$\text{and } OA = OA \text{ (common)}$$

$$\therefore \triangle OPA \cong \triangle OQA$$

Hence, $AP = AQ$.



Part II

In ΔAPQ

$AP = AQ$ (Proved)

$\therefore \angle 1 = \angle 2$ (Angles opposite to equal sides)

$\angle 1 + \angle 2 + \angle 3 = 180^\circ$ (Sum of angles of Δ 's) ... (i)

$\therefore \angle 4 = \angle 5$ (Angles opposite to radii)

$\angle 4 + \angle 5 + \angle 6 = 180^\circ$... (ii)

Adding (i) and (ii)

$$\angle 1 + \angle 2 + \angle 3 + \angle 4 + \angle 5 + \angle 6 = 360^\circ$$

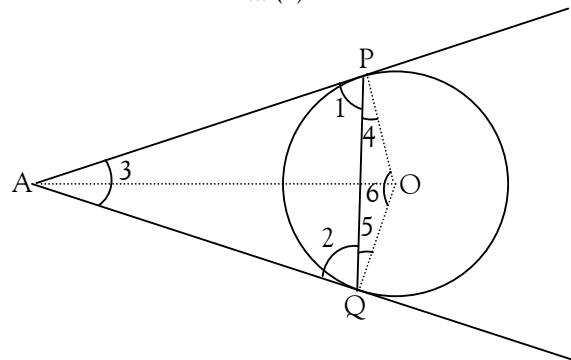
$$2\angle 1 + 2\angle 4 + \angle 3 + \angle 6 = 360^\circ$$

$$2(\angle 1 + \angle 4) + \angle 3 + \angle 6 = 360^\circ$$

$$2 \times 90^\circ + \angle 3 + \angle 6 = 360^\circ \quad (\text{as } OQ \perp AQ)$$

$$\angle 3 + \angle 6 = 360^\circ - 180^\circ = 180^\circ$$

$\angle 3$ and $\angle 6$ are supplementary



OR

The ratio of the areas of two similar triangles is equal to the ratio of the squares of the corresponding sides.

Given: ΔABC and ΔDEF are two similar triangles.

To prove:

$$(i) \quad \frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta DEF)} = \frac{BC^2}{EF^2} = \frac{AB^2}{DE^2} = \frac{AC^2}{DF^2}$$

Construction: Draw $AG \perp BC$ and $DH \perp EF$.

$$\text{Proof: (i)} \quad \frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta DEF)} = \frac{\frac{1}{2} \times BC \times AG}{\frac{1}{2} \times EF \times DH} = \frac{BC}{EF} \times \frac{AG}{DH} \dots (i)$$

$$(\because \text{area of } \Delta = \frac{1}{2} \text{ base} \times \text{height})$$

Now, in Δ s ABG and DEH , we have

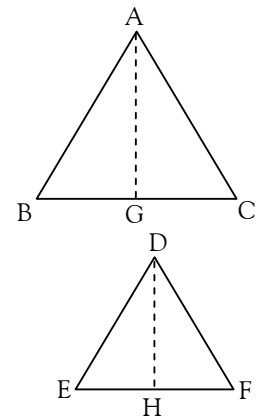
$$\angle B = \angle E \quad (\because \Delta ABC \sim \Delta DEF)$$

$$\angle AGB = \angle DHE \quad (\text{each equal to } 90^\circ)$$

$$\therefore \Delta ABG \sim \Delta DEH \quad (\text{AA Similarity})$$

$$\therefore \frac{AB}{DE} = \frac{AG}{DH}$$

(\because If Δ s are similar, the ratio of their corresponding sides is same)



But $\frac{AB}{DE} = \frac{BC}{EF}$ ($\because \Delta ABC \sim \Delta DEF$)

$\Rightarrow \frac{AG}{DH} = \frac{BC}{EF}$... (ii)

Now, from (i) and (ii), we have: $\frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta DEF)} = \frac{BC}{EF} \times \frac{BC}{EF} = \frac{BC^2}{EF^2}$

Similarly we can prove $\frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta DEF)} = \frac{BC^2}{EF^2} = \frac{AB^2}{DE^2} = \frac{AC^2}{DF^2}$... (1)

If the area of two similar triangle are equal i.e $\text{ar}(\Delta ABG) = \text{ar}(\Delta DEH)$

Using the above relation:

$$\frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta DEF)} = \frac{BC^2}{EF^2} = \frac{AB^2}{DE^2} = \frac{AC^2}{DF^2}$$

$$1 = \frac{BC^2}{EF^2} = \frac{AB^2}{DE^2} = \frac{AC^2}{DF^2}$$

We get $BC = EF$, $AB = DE$ and $DF = AC$

Now, in Δ s ABG and DEH , we have $BC = EF$, $AB = DE$ and $DF = AC$

$\therefore \Delta ABG \cong \Delta DEH$ (using SSS)

29. Radius of top $R = 28$ cm

Radius of bottom $r = 7$ cm

Let height of the bucket = h

Capacity of the bucket = 21560 cm^3

As capacity = $\frac{\pi h}{3} [R^2 + r^2 + Rr]$

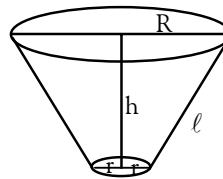
$$21560 = \frac{\pi h}{3} [R^2 + r^2 + Rr] = (22/7) (h/3) (28^2 + 7^2 + 28 \times 7)$$

$$21560 = 1078 h$$

$$h = 20$$

$$\text{Slant height of Frustum} = \sqrt{h^2 + (R - r)^2} = \sqrt{20^2 + (28 - 7)^2} = \sqrt{400 + 441} = \sqrt{841} = 29$$

$$\text{Total surface area} = \pi [\ell (R + r) + r^2] = 3344 \text{ cm}^2$$



Classes	Frequency (f_i)	Class mark x_i	$f_i x_i$	Cumulative frequency
10 - 20	4	15	60	4
20 - 30	8	25	200	12
30 - 40	10	35	350	22
40 - 50	12	45	540	34
50 - 60	10	55	550	44
60 - 70	4	65	260	48
70 - 80	2	75	150	50
	$\sum f_i = 50$		$\sum f_i x_i = 2110$	

$$\text{Mean} = \frac{\sum f_i x_i}{\sum f_i} = \frac{2110}{50} = 42.20$$

Calculation of median

Since $n = 50$.

So, $\frac{n}{2} = \frac{50}{2} = 25$ This observation lies in 40 - 50.

$\therefore \ell = 40, f = 12, cf = 22, h = 10$

$$\text{We know, median} = \ell + \left(\frac{\frac{n}{2} - cf}{f} \right) \times h = 40 + \left(\frac{\frac{50}{2} - 22}{12} \right) \times 10 = 40 + 2.5 = 42.5$$

Calculation of mode

Here the maximum class frequency is 12 and the class corresponding to this frequency is 40 - 50

So, modal class is 40 - 50

Lower limit (ℓ) of modal class = 40

Frequency (f_1) of modal class = 12

Frequency (f_0) of class preceding modal class = 10

Frequency (f_2) of class succeeding modal class = 10

$$\text{We know, Mode} = \ell + \left(\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right) \times h = 40 + \left[\frac{(12 - 10)}{2 \times 12 - 10 - 10} \right] \times 10 = 40 + \frac{2 \times 10}{4} = 40 + 5 = 45.$$