

# MODEL SOLUTIONS TO IIT JEE 2008

## PAPER 2

### CODE - 0

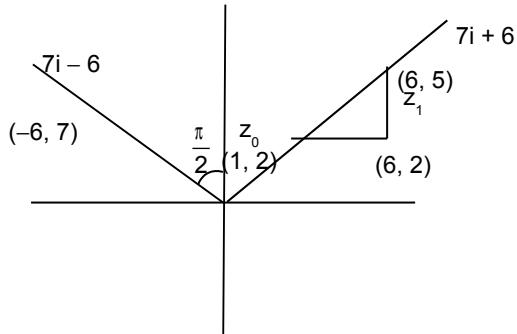
#### PART I

1	2	3	4	5	6	7	8	9	10
<b>D</b>	<b>C</b>	<b>B</b>	<b>B</b>	<b>D</b>	<b>D</b>	<b>A</b>	<b>C</b>	<b>A</b>	<b>C</b>
11	12	13	14	15	16	17	18	19	
<b>A</b>	<b>C</b>	<b>C</b>	<b>A</b>	<b>A</b>	<b>B</b>	<b>B</b>	<b>D</b>	<b>C</b>	

20	21	22
<b>A - s</b>	<b>A - r</b>	<b>A - p</b>
<b>B - p, q</b>	<b>B - q, s</b>	<b>B - s</b>
<b>C - r</b>	<b>C - r</b>	<b>C - q</b>
<b>D - p, q, s</b>	<b>D - p, r</b>	<b>D - q</b>

#### Section I

1.



$\Rightarrow (d)$

$$2. \quad g(u) = 2\tan^{-1}(e^u) - \frac{\pi}{2}$$

$$\Rightarrow g'(u) = \frac{2}{1+e^{2u}} e^u$$

$$g'(-u) = \frac{2e^{-u}}{1+e^{-2u}} = \frac{2e^{2u}}{e^u(1+e^{2u})}$$

$$= \frac{2e^u}{1+e^{2u}} = g'(u)$$

$\therefore g'(u)$  is even function

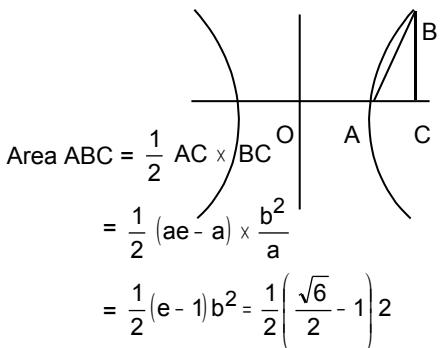
$\therefore g(u)$  is odd.

But  $g'(u) > 0 \Rightarrow$  strictly increasing in  $(-\infty, \infty)$   
 $\Rightarrow (c)$

$$3. \quad \frac{(x - \sqrt{2})^2}{4} - \frac{(y + \sqrt{2})^2}{2} = 1$$

$$\Rightarrow a^2 = 4, e^2 = \frac{4+2}{4} = \frac{6}{4}$$

$$b^2 = 2$$



$$= \frac{1}{2}(\sqrt{6} - 2) = \frac{\sqrt{6}}{2} - 1 = \frac{\sqrt{3}}{\sqrt{2}} - 1$$

$\Rightarrow$  (b)

$$\begin{aligned} 4. \quad & \int_0^{\pi/4} (y_1 - y_2) dx \\ &= \int_0^{\pi/4} \left( \sqrt{\frac{1+\sin x}{\cos x}} - \sqrt{\frac{1-\sin x}{\cos x}} \right) dx \\ &\text{sinx} = \frac{2t}{1+t^2}; \quad \cos x = \frac{1-t^2}{1+t^2}; \\ &= \int_0^{\sqrt{2}-1} \left( \sqrt{\frac{2t}{1+t^2}} - \sqrt{\frac{1-2t}{1+t^2}} \right) \frac{2dt}{1+t^2} \\ &= \int_0^{\sqrt{2}-1} \frac{2t}{(1+t^2)\sqrt{1-t^2}} \cdot 2dt \\ &= \int_0^{\sqrt{2}-1} \frac{4t}{(1+t^2)\sqrt{1-t^2}} dt \\ &\Rightarrow \text{(b)} \end{aligned}$$

$$\begin{aligned} 5. \quad & \text{Take } \alpha = \frac{\pi}{8}, \beta = \frac{\pi}{8}, \theta = \frac{\pi}{8} \\ & \Rightarrow P \left( -\sin 0, -\cos \frac{\pi}{8} \right) = P \left( 0, -\cos \frac{\pi}{8} \right) \\ & Q \left( \cos 0, \sin \frac{\pi}{8} \right) = Q \left( 1, \sin \frac{\pi}{8} \right) \\ & R \left( \cos \frac{\pi}{8}, \sin 0 \right) = R \left( \cos \frac{\pi}{8}, 0 \right) \\ & \text{RQ} \Rightarrow \frac{y - \sin \frac{\pi}{8}}{\sin \frac{\pi}{8}} = \frac{x - 1}{1 - \cos \frac{\pi}{8}} \end{aligned}$$

Substituting P in RQ  $\Rightarrow$  P does not lie on RQ.

$$PR \Rightarrow \frac{y - 0}{\cos \frac{\pi}{8}} = \frac{x - \cos \frac{\pi}{8}}{\cos \frac{\pi}{8}}$$

Substituting Q in PR  $\Rightarrow$  Q does not lie on PR.

$$PQ \Rightarrow \frac{y - \sin \frac{\pi}{8}}{\sin \frac{\pi}{8} + \cos \frac{\pi}{8}} = \frac{x - 1}{1}$$

Substituting R in PQ  $\Rightarrow$  R does not lie on PQ.

$\Rightarrow$  P, Q, R are not collinear.

$\Rightarrow$  (d)

6. Let  $n(B \text{ only}) = y$

$$n(A \cap B) = x$$

Then  $n(A \text{ only}) = 4 - x$

$$\therefore P(A \cap B) = \frac{x}{10}$$

$$P(A) = \frac{4}{10} \text{ and } P(B) = \frac{x+y}{10}$$

$\therefore P(A \cap B) = P(A) P(B)$

$$\Rightarrow \frac{x}{10} = \frac{x+y}{10} \times \frac{4}{10}$$

$$\Rightarrow 3x = 2y$$

$\Rightarrow (x+y)$  is a multiple of 5.

Only possible values are 5 and 10.

$\Rightarrow$  (d)

7.  $\bar{a} = i, \bar{b} = \cos \alpha i + \sin \alpha j, \alpha \text{ acute}$

$$\bar{r} = i \cos t + \sin t (\cos \alpha i + \sin \alpha j)$$

$$r = \sqrt{(\cos t + \sin t \cos \alpha)^2 + \sin^2 t \sin^2 \alpha}$$

$$\begin{aligned} &= \sqrt{\cos^2 t + 2 \cos t \sin t \cos \alpha + \sin^2 t \cos^2 \alpha + \sin^2 t \sin^2 \alpha} \\ &= \sqrt{1 + \cos \alpha \sin 2t} \end{aligned}$$

$$\text{Max} \Rightarrow \sqrt{1 + \cos \alpha}$$

$$1 + \bar{a} \cdot \bar{b} = 1 + \cos \alpha$$

$$\Rightarrow \text{Max} = \sqrt{1 + ab} = [1 + (\bar{a} - \bar{b})]^{1/2}$$

$$\sin 2t = \sin \frac{\pi}{2} \Rightarrow t = \frac{\pi}{4}$$

$$\begin{aligned} \Rightarrow \hat{u} &= \bar{a} \cdot \cos \frac{\pi}{4} + \bar{b} \cdot \sin \frac{\pi}{4} = \frac{1}{\sqrt{2}} (\bar{a} + \bar{b}) \\ &= \frac{\bar{a} + \bar{b}}{|\bar{a} + \bar{b}|} \end{aligned}$$

$\therefore$  (a)

$$8. \quad J = \int \frac{e^{3x}}{e^{4x} + e^{2x} + 1} dx$$

$$I = \int \frac{e^{3x} - e^x}{e^{4x} + e^{2x} + 1} dx$$

$$= \int \frac{e^x - e^{-x}}{e^{2x} + e^{-2x} + 1} dx$$

$$u = e^x + e^{-x} \Rightarrow du = (e^x - e^{-x})dx$$

$$u^2 = e^{2x} + e^{-2x} + 2$$

$$\int \frac{du}{u^2 - 1} = \frac{1}{2} \log \frac{u-1}{u+1} + 1$$

$$= \frac{1}{2} \log \left| \frac{e^x + e^{-x} - 1}{e^x + e^{-x} + 1} \right| + C$$

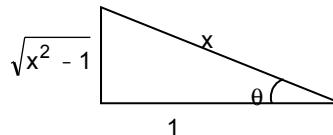
$$\begin{aligned}
&= \frac{1}{2} \log \left| \frac{e^{2x} - e^x + 1}{e^{2x} + e^x + 1} \right| + C \\
&\Rightarrow (c) \\
9. \quad g(x) &= \log_e f(x) \quad f(x+1) = x \cdot f(x) \\
f(x) &= e^{g(x)} \\
f(x+1) &= e^{g(x+1)} = x \cdot e^{g(x)} \\
e^{g(x+1)-g(x)} &= x \\
g(x+1) - g(x) &= \log x \\
g(x+1) &= g(x) + \log x \quad (1) \\
g'(x+1) &= g'(x) + \frac{1}{x} \\
g''(x+1) &= g''(x) - \frac{1}{x^2} \quad (2) \\
x+1 &= N + \frac{1}{2} \Rightarrow x = N - \frac{1}{2} \\
\therefore (1) \Rightarrow g''\left(N + \frac{1}{2}\right) - g''\left(N - \frac{1}{2}\right) &= \frac{-1}{\left(N - \frac{1}{2}\right)^2} \\
\Sigma &= \frac{-1}{\left(1 - \frac{1}{2}\right)^2} - \frac{1}{\left(2 - \frac{1}{2}\right)^2} - \frac{1}{\left(3 - \frac{1}{2}\right)^2} - \dots \\
&= -1 \left[ \frac{1}{\frac{1}{4}} + \frac{1}{\frac{9}{4}} + \frac{1}{\frac{25}{4}} + \dots \right] \\
&= -4 \left[ \frac{1}{1} + \frac{1}{3^2} + \frac{1}{5^2} + \dots + \frac{1}{(2N-1)^2} \right] \\
\Rightarrow (a)
\end{aligned}$$

## Section II

10.  $b_1 = a_1$   
 $b_2 = a_1 + a_1 r, b_3 = a_1 + a_1 r + a_1 r^2$   
 $b_4 = a_1 + a_1 r + a_2 r^2 + a_3 r^3$   
They are neither in A.P. nor G.P  
 $\therefore$  Statement 1 is true  
 $b_1, b_2, b_3, b_4$  are not in H.P  
 $\therefore$  Statement 2 is false  
 $\therefore \Rightarrow (c)$

11.  $x^2 + 2px + q = 0$  and  $ax^2 + 2bx + c = 0$  have common root  
 $\therefore \frac{\alpha^2}{2pc - 2pq} = \frac{\alpha}{aq - c} = \frac{1}{2b - 2ap}$   
Again  $x^2 + 2px + q = 0$  and  $cx^2 + bx + a = 0$  have common root  
 $\frac{\beta^2}{2ap - 2bq} = \frac{\beta}{cq - a} = \frac{1}{2b - 2pc}$   
By using statement (2)  $\alpha, \beta$  are real  
 $\therefore (p^2 - q) > 0$  and  $b^2 - ac > 0$   
 $\therefore (p^2 - q)(b^2 - ac) > 0$

- $\therefore \Rightarrow (a)$
12. Statement 1:  
Centre of the circle is at  $(-3, 5)$   
Radius = 2  
If  $L_1$  is a chord of the circle  
 $2 \times -3 + 3 \times 5 + p - 3 \neq 0$   
 $p + 6 \neq 0 \Rightarrow p \neq -6$   
If  $L_2$  is to be a diameter of the circle,  
 $2 \times -3 + 3 \times 5 + p + 3 = 0$   
 $p = -12$   
Statement 1 is true
- Statement 2 :  
 $L_1$  is a diameter of C  
 $\Rightarrow p$  lies on  $L_1$   
 $\Rightarrow -6 + 15 + p - 3 = 0$   
 $\Rightarrow p + 6 = 0$   
 $\Rightarrow p = -6$   
Now  
 $L_2 : 2x + 3y - 3 = 0$   
Perpendicular distance if  $L_2$  from  $p = \frac{6}{13} < 2$   
 $\therefore L_2$  is a chord always  
 $\therefore$  Statement 2 is false  
 $\Rightarrow (c)$

- 13.
- 
- $$\begin{aligned}
\frac{dy}{y\sqrt{y^2 - 1}} &= \frac{dx}{x\sqrt{x^2 - 1}} \\
\sec^{-1} y &= \sec^{-1} x + C \\
x = 2, y = \frac{2}{\sqrt{3}} & \\
\sec^{-1} \frac{2}{\sqrt{3}} &= \sec^{-1} 2 + C \\
\frac{\pi}{6} &= \frac{\pi}{3} + C \Rightarrow C = \frac{\pi}{6} - \frac{\pi}{3} = -\frac{\pi}{6} \\
\Rightarrow \sec^{-1} y &= \sec^{-1} x - \frac{\pi}{6} \\
y = \sec \left( \sec^{-1} x - \frac{\pi}{6} \right) & \quad (1)
\end{aligned}$$
- Statement 1 is true  
Consider the relation
- $$\begin{aligned}
\frac{1}{y} &= \frac{2\sqrt{3}}{x} - \sqrt{1 - \frac{1}{x^2}} = \frac{2\sqrt{3}}{x} - \frac{\sqrt{x^2 - 1}}{x} \\
&= \frac{2\sqrt{3} - \sqrt{x^2 - 1}}{x} \\
y &= \frac{x}{2\sqrt{3} - \sqrt{x^2 - 1}}
\end{aligned}$$
- From (1)

$$\begin{aligned} \frac{1}{y} &= \cos\left(\sec^{-1}x - \frac{\pi}{6}\right) \\ &= \cos(\sec^{-1}x)\cos\frac{\pi}{6} + \sin(\sec^{-1}x)\sin\frac{\pi}{6} \\ &= \cos\left(\cos^{-1}\frac{1}{x}\right)\frac{\sqrt{3}}{2} - \frac{\sqrt{x^2-1}}{2} \end{aligned}$$

Statement 2 is false

Statement 1 is true

$\Rightarrow (c)$

### Section III

$$\begin{aligned} 14. f(x) &= \frac{x^2 + ax + 1 - 2ax}{x^2 + ax + 1} \\ &= 1 - \frac{2ax}{x^2 + ax + 1} \\ f'(x) &= \frac{(x^2 + ax + 1)(-2a) + 2ax(2x + a)}{(x^2 + ax + 1)^2} \\ &= \frac{-2ax^2 - 2a^2x - 2a + 4ax^2 + 2a^2x}{(x^2 + ax + 1)^2} \\ &= \frac{2a(x^2 - 1)}{(x^2 + ax + 1)^2} \\ f'(x) &= \frac{(x^2 + ax + 1)^2[4ax] - 4a(x^2 - 1)}{(x^2 + ax + 1)(2x + a)} \\ f'(1) &= \frac{(2+a)^2 4a}{(2+a)^4} = \frac{4a}{(2+a)^2} \\ f'(-1) &= \frac{(2-a)^2 (-4a)}{(2-a)^4} = \frac{-4a}{(2-a)^2} \\ (2+a)^2 f'(1) + (2-a)^2 f'(-1) &= 0 \\ \Rightarrow (a) & \end{aligned}$$

$$15. f(x) = \frac{2a(x^2 - 1)}{(x^2 + ax + 1)^2}$$

Since  $a > 0$ ,  $x^2 - 1$  is  $< 0$

When  $x \in (-1, 1)$

$\Rightarrow (a)$

$$\begin{aligned} 16. g(x) &= \int_0^x \frac{f'(t)}{1+t^2} dt \\ \Rightarrow g'(x) &= \frac{f'(e^x)}{1+(e^x)^2} \times e^x \\ &= \frac{e^x}{1+(e^x)^2} \left\{ \frac{2a(e^{2x} - 1)}{(e^{2x} + ae^x + 1)^2} \right\} \\ \Rightarrow (b) & \end{aligned}$$

$$\begin{aligned} 17. (3\bar{i} + \bar{j} + 2\bar{k}) \times (\bar{i} + 2\bar{j} + 3\bar{k}) \\ &= \begin{vmatrix} \bar{i} & \bar{j} & \bar{k} \\ 3 & 1 & 2 \\ 1 & 2 & 3 \end{vmatrix} \\ &= -\bar{i} - 7\bar{j} + 5\bar{k} \\ \text{Unit vector} &= \frac{1}{5\sqrt{3}}(-\bar{i} - 7\bar{j} + 5\bar{k}) \\ \Rightarrow (b) & \end{aligned}$$

18. Shortest distance

$(-1, -2, -1) \rightarrow$  point on  $L_1$

$(2, -2, 3) \rightarrow$  point on  $L_2$

$$\begin{aligned} \text{Shortest distance} &= \frac{1}{5\sqrt{3}} \begin{vmatrix} 3 & 0 & 4 \\ 3 & 1 & 2 \\ 1 & 2 & 3 \end{vmatrix} \\ &= \frac{3(-1) + 4 \times 5}{5\sqrt{3}} = \frac{17}{5\sqrt{3}} \\ \Rightarrow (d) & \end{aligned}$$

19. Equation of the plane is

$$-1(x+1) - 7(y+2) + 5(z+1) = 0$$

$$-x - 7y + 5z - 10 = 0$$

$$x + 7y - 5z + 10 = 0$$

$$\text{Distance} = \frac{1+75+10}{\sqrt{75}} = \frac{13}{\sqrt{75}}$$

$\Rightarrow (c)$

### Section IV

$$\begin{aligned} 20. \begin{vmatrix} 1 & 3 & -5 \\ 3 & -k & -1 \\ 5 & 2 & -12 \end{vmatrix} \\ 12k + 2 - 3(-36 + 5) - 5(6 + 5k) = 0 \\ 12k + 2 + 108 - 15 - 30 - 25k = 0 \\ -13k + 65 = 0 \Rightarrow k = 5 \\ (a) \rightarrow s \\ (b) \rightarrow p, q \\ (c) \rightarrow r \end{aligned}$$

(d)  $\rightarrow$  p, q, s

21.

$$(A) y = \frac{x^2 + 2x + 4}{x + 2}$$

$$y' = \frac{(x+2)(2x+2) - (x^2 + 2x + 4)}{(x+2)^2}$$

$$= \frac{x^2 + 4x}{(x+2)^2}$$

$$y'' = \frac{(x+2)^2(2x+4) - (x^2 + 4x)2(x+2)}{(x+2)^4}$$

For extremum,  $y' = 0 \Rightarrow x = 0, -4$

At  $x = 0$ ,  $y'' > 0 \Rightarrow x = 0$  gives a min. pt & min. value = 2

At  $x = -4$ ,  $y'' < 0 \Rightarrow x = -4$  gives a max. pt & max. value = -6

$\therefore \Rightarrow (r)$

$$(B) (A + B)(A - B) = (A - B)(A + B)$$

$$\Rightarrow AB = BA \quad \dots(1)$$

$$(AB)^T = (-1)^k AB$$

$$\Rightarrow B^T A^T = (-1)^k BA \quad (\text{using 1})$$

$$-BA == (-1)^k BA$$

(because B is skew symmetric and A is symmetric)

$\Rightarrow k$  is an odd integer.

$\therefore k$  is 1 or 3

$\therefore \Rightarrow (q), (s)$

$$(C) a = \log_3 \log_3 2 \Rightarrow 3^a = \log_3 2$$

$$\Rightarrow 3^{-a} = \log_2 3$$

We have

$$1 < 2^{-k+3^{-a}} < 2$$

$$\Rightarrow 0 < -k + \log_2 3 < 1$$

$$\Rightarrow \log_2 3 - 1 < k < \log_2 3$$

$\Rightarrow$  Integer value that k takes is 1.

$\Rightarrow (r)$

$$(D) \sin \theta = \cos \varphi = \sin \left( \frac{\pi}{2} - \varphi \right)$$

$$\Rightarrow \theta = n\pi + (-1)^n \left( \frac{\pi}{2} - \varphi \right)$$

$$\text{For } n = 1, \text{ we get } \frac{\theta - \varphi - \frac{\pi}{2}}{\pi} = 0$$

$$\text{For } n = 2, \text{ we get } \frac{\theta + \varphi - \frac{\pi}{2}}{\pi} = 2$$

$\Rightarrow (p), (r).$

22.

(A) ENDEA is considered as 1 letter  
Remaining letters are E, N, O, L

So  $4 + 1 = 6$  letters  $\Rightarrow 5!$

$\Rightarrow (p)$

(B) E \_\_\_\_\_ E

The remaining letters are 2N, E, D, A, O, L

$$\text{Required number of permutations} = \frac{7!}{2!}$$

$$= 21 \times 5!$$

$\Rightarrow (s)$

(C) D, L, N can occur only in the first four places  
 $\Rightarrow$  D, L, N, N occurs in the first four places

$$\text{No. of ways} = \frac{4!}{2!} = 12$$

Remaining are 3E, A, 0, fill in the 5 places

$$\text{No. of ways} = \frac{5!}{3!} = 20$$

$$\text{Total no. of ways} = (5 \times 4 \times 3 \times 2) \times 2$$

$$= 2 \times 5!$$

$\Rightarrow (q)$

(D) X    X    X    X    X  
- - - - -

5 odd positions

A, E and O occur only in odd positions

$$\therefore A, E, E, E, O \text{ occupy 5 places} = \frac{5!}{3!} = 20$$

Remaining 4 places are filled by

$$N, N, L, D \text{ in } \frac{4!}{2!} \text{ ways} = 12$$

$$= 2 \times 5!$$

$\Rightarrow (q)$

## PART II

23 <b>C</b>	24 <b>A</b>	25 <b>A</b>	26 <b>C</b>	27 <b>D</b>	28 <b>B</b>	29 <b>A</b>	30 <b>A</b>	31 <b>B</b>	32 <b>B</b>
33 <b>D</b>	34 <b>B</b>	35 <b>C</b>	36 <b>A</b>	37 <b>B</b>	38 <b>C</b>	39 <b>D</b>	40 <b>D</b>	41 <b>C</b>	

42

**A – p**

**B – q, r, s**

**C-s**

**D-q**

43

**A – p, q, r, s**

**B – q**

**C-p, q, r, s**

**D-p, q, r, s**

44

**A – q**

**B – p, r**

**C – p, s**

**D – q, s**

### Section I

23.  $F = \frac{1}{4\pi\epsilon_0} \frac{q/3 \times 2q/3}{(\sqrt{3}R)^2}$

24.  $\lambda_1 = \frac{1}{4} \lambda_2$

25. P moves up implies direction  $\hat{j}$

26.  $\frac{1}{2}kx^2 = \frac{1}{2}4ky^2$

27.  $v^2 = u^2 - 2gh; u^2 = 5gR$

$$\Rightarrow v^2 = \frac{u^2}{4} \Rightarrow h = \frac{15}{8}R$$

28.  $P_1 = \frac{4T}{R}; P_2 < \frac{4T}{R}$

air flowing from 1 to 2 equalizing pressure.

29.  $\frac{3\lambda}{4} = 0.75 \Rightarrow \lambda = 1 \text{ m}$

$f = 340 \text{ Hz}; T$  increases  $f$  increases; beat decreases  $\Rightarrow n = 340 + 4$

30.  $C = \frac{\epsilon_0 A}{(d-x) + \frac{x}{K}}$

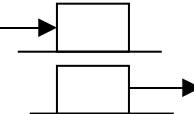
$$x = \frac{d}{3}vt$$

31. Only region I and IV are to be reckoned for TIR.

### Section II

32. Relative angular velocity is inversely proportional to distance.

33.



Pushing or pulling does not imply any angle. Hence to be taken as horizontal. Thus statement -1 is wrong

34. For earth radius is large; never zero potential.

35. Soft iron is easy to magnetize / demagnetize

### Section III

36.  $E = \frac{1}{4\pi\epsilon_0} \frac{Ze}{R^2}$

37.  $\rho = d \left(1 - \frac{r}{R}\right)$   
 $\int \rho 4\pi r^2 dr = Ze$

38. Standard E variation for uniform sphere

39.  $2kxR = I\alpha = \frac{3}{2}MR^2 \frac{a}{R}$

$$Ma = \frac{4}{3}kx$$

40.  $\omega = \sqrt{\frac{4k}{3M}}$

41.  $f = I_{CM}\alpha = \frac{Ma}{2} = \frac{2}{3}kx$

$$\frac{2}{3}kA = \mu mg$$

$$2\frac{1}{2}kA^2 = \frac{1}{2}I_0^2$$

## Section IV

42.

- (A) Potential energy graph is a parabola, with minimum at  $x = x_0$ .

- (B) q is motion with zero acceleration starting from origin ( $y = 0$ )  
 r is zero acceleration starting from ( $y = y_0$ )  
 s is constant acceleration.

(C)  $R = \frac{u^2 \sin 2\theta}{g}$  for same  $\theta$ ,  $R \propto u^2 \Rightarrow$  Parabola

passing through the origin.

$\Rightarrow (s)$

(D)  $T = 2\pi \sqrt{\frac{\ell}{g}}$

$T^2 \propto \ell$

$\Rightarrow$  Straight line passing through origin.

$\Rightarrow (q)$

43. A, C, D

If  $|u| < |f| \Rightarrow$  virtual image

If  $|u| > |f| \rightarrow$  Real image, magnified

If  $|u| = |f| \rightarrow$  Image at infinity

$\Rightarrow p, q, r, s$

- (B) For all  $u$ , virtual, diminished image  
 $\Rightarrow q$

44.

- (A) Free expansion for ideal gas in insulated container, internal energy remains constant, temperature remains constant, and no heat loss.

$\Rightarrow (q)$

For  $pV^n = \text{constant process.}$

$$\begin{aligned} \Delta Q &= \Delta U + \Delta W \\ &= \frac{\Delta(pV)}{\gamma - 1} - \frac{\Delta(pV)}{n - 1} \\ &= \Delta(nRT) \left( \frac{1}{\gamma - 1} - \frac{1}{n - 1} \right) \end{aligned}$$

If  $n > 1, \Delta T < 0$

If  $n > \gamma, \Delta Q < 0$

$n < \gamma, \Delta Q > 0$

- (B)  $n = 2 \quad p, r$

- (C)  $n = \frac{4}{3} \quad p, s$

- (D)  $\Delta Q = \Delta U + \Delta W$

From fig.  $\Delta W > 0$

$\Delta T > 0 \Rightarrow \Delta U > 0$

$\Rightarrow \Delta Q > 0$

$\Rightarrow q, s$

### PART III

45	46	47	48	49	50	51	52	53	54
<b>D</b>	<b>A</b>	<b>C</b>	<b>C</b>	<b>B</b>	<b>C</b>	<b>B</b>	<b>A</b>	<b>D</b>	<b>D</b>
55	56	57	58	59	60	61	62	63	
<b>A</b>	<b>B</b>	<b>A</b>	<b>B</b>	<b>A</b>	<b>D</b>	<b>B</b>	<b>A</b>	<b>D</b>	

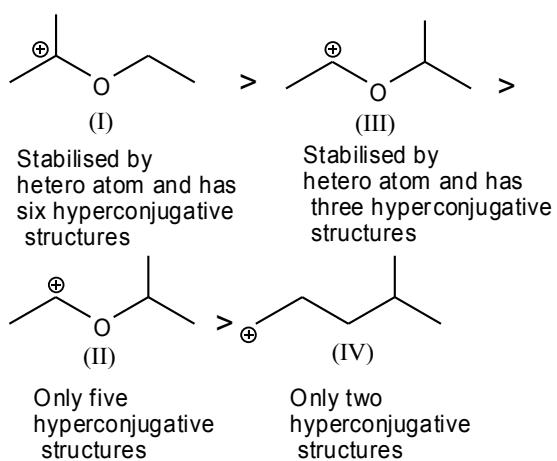
- 64  
**A – r, s**  
**B – p, q**  
**C – p, q, r**  
**D – p, s**

- 65  
**A – p**  
**B – q**  
**C – p, r**  
**D – p, s**

- 66  
**A – q**  
**B – p**  
**C – p, q, r**  
**D – p, q**

### Section I

45. (I) > (III) > (II) > (IV)

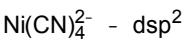


46. Cellulose has a  $\beta$ -glycosidic linkage. While structures (A) and (B) have  $\beta$  glycosidic linkages, only the structure (A) is a triacetate.

47. is a  $\beta$  keto acid which undergoes readily decarboxylation to give  $\text{C}_6\text{H}_5\text{COCH}_3$  which is (E). (E) undergoes iodoform reaction to give (F) which is  $\text{C}_6\text{H}_5\text{COONa}$  and (G) which is  $\overset{*}{\text{CHI}}_3$ .

48.  $\text{CuF}_2$  is coloured because  $\text{Cu}^{2+}$  with  $d^9$  configuration is the cation.

49.  $[\text{Ni}(\text{CO})_4] - \text{sp}^3$



50. Tetraammine nickel (II)–tetrachloronickelate (II)

$$\begin{aligned} 51. 1 \text{ mole of hydrogen} &= 2 \text{ equivalents} \\ 0.1 \text{ mole of hydrogen} &= 0.02 \text{ equivalents} \\ \text{Current required} &= 0.02 \text{ F} \\ &= 0.02 \times 96500 \text{ C} \\ \text{Time (Sec)} &= \frac{0.02 \times 96500}{10 \times 10^{-3}} \\ &= 19.3 \times 10^4 \end{aligned}$$

52. Surfactant molecules with larger hydrophobic end will have lesser solubility, greater tendency to associate and hence form micelles readily.

$$\begin{aligned} 53. \text{MX : } K_{\text{sp}} = S^2 &\quad S = \sqrt{4 \times 10^{-8}} \\ \text{MX}_2 : K_{\text{sp}} = 4S^3 &\quad S = 3\sqrt{\frac{3.2 \times 10^{-14}}{4}} \\ \text{M}_3\text{X} : K_{\text{sp}} = 27S^4 &\quad S = 4\sqrt{\frac{2.7 \times 10^{-15}}{27}} \\ \text{MX} > \text{M}_3\text{X} > \text{MX}_2 \end{aligned}$$

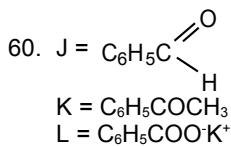
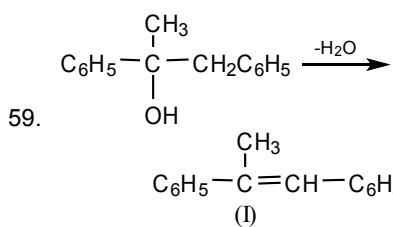
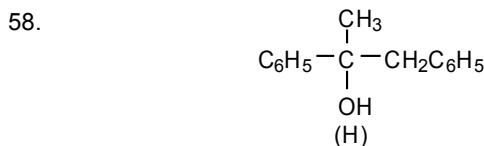
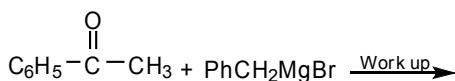
### Section II

54. Statement (1) is not correct as an orange red dye is formed. Statement (2) is true because the red colour is due to extended conjugation

55. Statement (1) is true and statement (2) is also true and is correct explanation for statement (1). In  $[\text{Fe}(\text{H}_2\text{O})_5\text{NO}]^{2+}$ , Fe is in +1 state with 3 unpaired electrons.

56. Statement (1) is true and statement (2) is also true but statement (2) is not the correct explanation of statement (1).  
These geometrical isomers are optically inactive as they have plane of symmetry. A molecule may be optically active even if it has axis of symmetry.  
57. The natural asymmetry between the conversion of heat and work is due to the fact that heat cannot be completely converted to work.

### Section III



61. Effective number of particles in HCP =

$$\frac{1}{6} \times 12 + \frac{1}{2} \times 2 + 3 = 6$$

62. Volume of Unit cell =  $6 \times \frac{\sqrt{3}}{4} (2r)^2 \times 4r \sqrt{\frac{2}{3}}$   
 $= 24\sqrt{2} r^3$

63. PF = 0.74  
VF = 0.26

### Section IV

64. (A)  $\rightarrow$  R, S  
(B)  $\rightarrow$  P, Q  
(C)  $\rightarrow$  P, Q, R  
(D)  $\rightarrow$  P, S

(A) It has no carbon and hence the sodium fusion extract does not give blue colour with  $\text{FeSO}_4$ .

No phenolic -OH group, hence does not give  $\text{FeCl}_3$  test.

Gives white ppt. of  $\text{AgCl}$  with  $\text{AgNO}_3$ .  
Forms Hydrazone with aldehydes as it has hydrazine content.

- (B) Forms Prussian blue.  
Gives positive  $\text{FeCl}_3$  test as it has phenolic -OH group.  
Gives yellow ppt. of  $\text{AgI}$  with  $\text{AgNO}_3$ .  
Does not form hydrazone as there is no hydrazine content.

- (C) Forms Prussian blue.  
Gives positive  $\text{FeCl}_3$  test as there is phenolic -OH group.  
Gives white ppt. of  $\text{AgCl}$  with  $\text{AgNO}_3$ .  
Does not form hydrazone as there is no hydrazine content.

- (D) Forms Prussian blue.  
No phenolic -OH group, hence does not give  $\text{FeCl}_3$  test.  
Give pale yellow ppt. of  $\text{AgBr}$  with  $\text{AgNO}_3$ .  
Forms Hydrazone with aldehydes as it has hydrazine content.

65. (A)  $\rightarrow$  P  
(B)  $\rightarrow$  Q  
(C)  $\rightarrow$  P, R  
(D)  $\rightarrow$  P, S

(A)  $\text{PbS}$  is converted to  $\text{PbO}$  by roasting  
 $2\text{PbS} + 3\text{O}_2 \rightarrow 2\text{PbO} + 2\text{SO}_2$

(B)  $\text{CaCO}_3$  on calcination gives  $\text{CaO}$   
 $\text{CaCO}_3 \rightarrow \text{CaO} + \text{CO}_2$

(C)  $\text{ZnS}$  is converted to  $\text{Zn}$  either by roasting followed by carbon reduction.  
 $2\text{ZnS} + 3\text{O}_2 \rightarrow 2\text{ZnO} + 2\text{SO}_2$   
 $\text{ZnO} + \text{C} \rightarrow \text{Zn} + \text{CO}$

(D)  $\text{Cu}_2\text{S}$  to  $\text{Cu}$  involves roasting and self reduction  
 $2\text{Cu}_2\text{S} + 3\text{O}_2 \rightarrow 2\text{Cu}_2\text{O} + 2\text{SO}_2$   
 $\text{Cu}_2\text{S} + 2\text{Cu}_2\text{O} \rightarrow 6\text{Cu} + \text{SO}_2$

66. (A)  $\rightarrow$  Q  
(B)  $\rightarrow$  P  
(C)  $\rightarrow$  P, Q, R  
(D)  $\rightarrow$  P, Q  
(A) Orbital angular momentum of the electron in

$$\text{a hydrogen like A. O} = \sqrt{l(l+1)} \frac{h}{2\pi}$$

(B) A hydrogen – like are electron wave function obeying Pauli's principle : Principle quantum number.

- (C) Size, shape and orientation of orbital : Principle azimuthal and magnetic quantum numbers.
- (D) Probability density of the electron at the nucleus : Principal and azimuthal quantum number.